LogicBlox is a popular Datalog engine. You can write and query Datalog programs via its web interface, which is publicly available at

https://repl.logicblox.com

You will use this interface for all tasks in this exercise.

To illustrate LogicBlox, let’s encode the “family tree” example that you have seen in the lecture. When writing Datalog programs in LogicBlox, one needs to explicitly declare the argument types of input relations. The following rule declares that the argument types of the relation parent are String:

```
addblock 'parent(X, Y) -> string(X), string(Y).'
```

You can copy and paste the above block directly into the LogicBlox web interface.

Next, we can add two tuples to the parent relation:

```
exec '+parent("bob", "alice").
+parent("dave", "bob").'
```

We can then define the ancestor relation, called anc, as the transitive closure of the parent relation:

```
addblock 'anc(X, Y) <- parent(X, Y).
anc(X, Y) <- parent(X, Z), anc(Z, Y).'
```

Finally, we can query the fixed point of the Datalog program. For instance, to print which tuples are contained in anc relation, you can run the command print anc.
Problem 1. In this task, you will use stratified Datalog to verifying a network configuration. We consider a network that consists of 4 routers—A, B, C, and D. Our network carries traffic for three neighbor networks—N1, N2, and N3. The network topology is shown in Figure 1. Each links is associated with a weight (shown in Figure 1). Each router computes its own forwarding entries according to its local configuration, by running the OSPF protocol and composing the computed OSPF routes with any static routes defined in the configuration. OSPF is an intra-domain routing protocol used by routers to compute forwarding entries directing traffic to any internal destinations along the shortest-path based on configurable link weights. Each router composes the routes computed OSPF with those statically defined in the configuration based on the local preference configured in the router’s configuration. For our example network, the routers assign the local preference 10 to static routes and 5 to OSPF (i.e., routers would select any static route, if defined, over the computed OSPF routes). Router A has a static route that specifies that packets destined to network N3 must be forwarded to router B. The global forwarding plane of the network can be captured with a relation Fwd(Router, Network, NextHop). For example, the tuple Fwd(A, N2, D) captures that router A forwards packets destined to network N2 to router D.

Task 1: Encode the network configuration as a Datalog input. Define several relation that captures the network configuration. Relevant pieces of information that you must capture include: (1) network links and their costs, (2) the local preference of each router, and (3) static routes defined in the router configurations. Define the necessary relations using the LogicBlox syntax.
**Task 2: Encode network behavior**  Write a Datalog program that encodes how routers compute their forwarding entries. You must first specify how routers compute their OSPF routes (based on shortest path) and then specify how OSPF routes are composed with any statically defined entries (based on the router’s local preference). Your Datalog program must define the global forwarding plane of the network, i.e. the relation Fwd(Router, Network, NextHop).

**Task 3: Query the network’s forwarding plane**  Show the routers’ forwarding tables.

**Task 4: Check traffic isolation for networks N_2 and N_3**  Write a Datalog query that is satisfied if and only if

\[ \forall X,Y. (Fwd(X, N_2, Y) \Rightarrow (\neg Fwd(X, N_3, Y))) \]

Here, N_2 and N_3 denote the identifiers of the two networks. This property captures that the forwarding paths for networks N_2 and N_3 do not share links in the same direction.

**Task 5: Change the network configuration**  Change the router’s configuration so that the traffic isolation property for N_2 and N_3 holds.

**Problem 2. (Bonus problem)** In this task, you will use Datalog to declaratively specify a popular data-flow analysis, called reaching definitions. This analysis statically determines which assignments (a.k.a. definitions) may reach a given program label. For more information about the reaching definitions analysis and examples see [https://en.wikipedia.org/wiki/Reaching_definition](https://en.wikipedia.org/wiki/Reaching_definition).

To analyze a program in Datalog, we must first derive facts about the program, which capture information relevant for our analysis. For the reaching definitions analysis, we need information about (1) assignments and (2) control flow. We capture these pieces of information with the following two predicates:

1. `assign(Lab, Var)`, which captures that the program makes an assignment to variable Var at program label Lab
2. `follows(Lab1, Lab2)`, which captures that program label Lab1 is followed by Lab2

To illustrate how these relations are used to capture information about the program under analysis, consider the following simple program:

```java
public String name (String type){
```
```java
String a = "Anonymous";
if (type.equals("cat"))
a = "Garfield";
else if (type.equals("dog"))
a = "Snoopy";
else
    a = "Blob";
return a;
```

The input facts derived for this program are as follows:

- assign(1, "a") follows(1,2) follows(4,7)
- assign(3, "a") follows(2,3) follows(3,8)
- assign(5, "a") follows(2,4) follows(5,8)
- assign(7, "a") follows(4,5) follows(7,8)

**Task 1: Specify reaching definitions in Datalog** Specify the reaching definitions program analysis in Datalog (using the LogicBlox syntax). The resulting Datalog program must define the predicate `reach(Lab1, Var, Lab2)`, which is derived if and only if the assignment to the variable `Var` at label `Lab1` reaches label `Lab2`.

**Task 2: Find the set of reaching definitions** Show all reaching definitions for our example. To get the reaching definitions, you can run your Datalog program that you have encoded in Task 1.